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A STOCHASTIC FRONTIER ANALYSIS OF OUTPUT LEVEL AND GROWTH IN POLAND AND WESTERN ECONOMIES

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ABSTRACT: This paper uses Bayesian stochastic frontier methods to measure the productivity gap between Poland and Western countries that existed before the beginning of the main Polish economic reform. Using data for 20 Western economies, Poland and Yugoslavia (1980-1990) we estimate a translog stochastic frontier and make inference about individual efficiencies. Following the methodology proposed in our earlier work, we also decompose output growth into technical, efficiency and input changes and examine patterns of growth in the period under consideration.

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1. Introduction

Estimating the productivity gap between countries from both sides of the former "iron curtain", as well as comparing their growth patterns, is one of the important methodological problems related to the East-West European integration. In this paper we apply the Bayesian stochastic frontier framework, developed in Koop, Osiewalski and Steel (1997b) [hereafter KOS] to model output levels and growth rates in 22 countries under the assumption that there exists a common technology which defines the "world frontier" ("frontier" here meaning the maximum technically feasible output given inputs). We measure the distance between the actual output and its projection onto the theoretical world frontier. The latter distance measures the efficiency gap with respect to the production possibilities. We focus attention on Poland, but we also include Yugoslavia in our empirical study. The choice of these two countries, as well as the time period (1980-1990), was determined by the availability of comparable capital stock data. We use the Penn World Tables (Version 5.6) where the relevant data for East European countries are very limited.

In this paper, the idea of a production frontier is applied in a macroeconomic context in which countries are producers of output (e.g. GDP) given inputs (e.g. capital and labor). Accordingly, countries can be thought of as operating either on or within the frontier; and the distance from the frontier as reflecting inefficiency. Over time, a country can become less inefficient and "catch up" to the frontier or the frontier itself can shift over time, indicating technical progress. In addition, a country can move along the frontier by changing inputs. Hence, output growth can be thought of in terms of three different components: efficiency change, technical change and input change. Economists often refer to the first two components collectively as "productivity change".

Färe, Grosskopf, Norris and Zhang (1994) use Data Envelopment Analysis (DEA) to construct a frontier model for growth comparisons. DEA is a nonparametric methodology which assumes that the frontier is piecewise linear and no measurement error exists. In KOS we developed an alternative technique using a stochastic frontier model. Such models were pioneered by Meeusen and van den Broeck (1977) and Aigner, Lovell and Schmidt (1977). In KOS we argued that, at least for small, noisy data sets such as typically exist in the growth

literature, stochastic frontier methods have several advantages.¹

To estimate the stochastic frontier model considered in this paper we use Bayesian methods proposed in KOS. A justification for the use of Bayesian methods is given in our previous work (e.g. van den Broeck, Koop, Osiewalski and Steel (1994)). In particular, the adoption of a Bayesian stochastic frontier approach enables us to: i) Obtain exact small sample results in a way that is particularly appropriate for the treatment of this paper's very small data set. ii) Focus on any quantity of interest and derive its full posterior distribution; and in particular, the full posterior distribution of any individual efficiency or any function of the parameters and the data. iii) Easily integrate out nuisance parameters since each is assigned a probability distribution. Thus, we can take into account parameter uncertainty, a characteristic which is bound to be important since the small sample size will tend to prohibit precise estimation. iv) Easily impose (unlike classical methods) economic regularity conditions on the production function. Fernández, Osiewalski and Steel (1997) briefly discuss some aspects of classical estimation procedures.

We use recently developed numerical methods based on Markov chain random sampling, in particular, the Gibbs sampler (see e.g. Gelfand and Smith (1990)), to conduct the actual calculations. Note that our models can be easily handled using a personal computer.

The remainder of the paper is organized as follows: Section 2 defines the frontier model and the basic decomposition of output growth. Section 3 presents our Bayesian model and inference technique. Our empirical results are discussed in Section 4, and Section 5 concludes.

2. Modeling Output and Decomposing Growth

If we let Y_{it} , K_{it} and L_{it} be real output, capital stock and labor in period t ($t=1,...,T$) in country i ($i=1,...,N$), respectively, and assume a common world frontier f_t , evolving over time, then the model we consider takes the form:

¹In KOS we used Version 5.5 of the Penn World Tables (and examined 17 OECD countries over the period 1979-1988) in order to retain full comparability with Färe et al. (1994). Version 5.6, used in this study, is a substantial revision of the previous data set.

$$Y_{ti} = f_t(K_{ti}, L_{ti}) \tau_{ti} w_{ti}, \quad (1)$$

where τ_{ti} is the efficiency (i.e. $0 < \tau_{ti} \leq 1$ and $\tau_{ti} = 1$ implies full efficiency) and w_{ti} reflects the stochastic nature of the frontier itself (due to, e.g., measurement error). Throughout this paper, we assume a translog production frontier. Under this assumption a loglinear model based on (1) is obtained:

$$y_{ti} = x'_{ti} \beta_t + v_{ti} - u_{ti}, \quad (2)$$

where $u_{ti} = -\ln(\tau_{ti})$ is a nonnegative random variable, $v_{ti} = \ln(w_{ti})$ and is assigned a symmetric distribution with mean zero,

$$x_{ti} = (1 \quad k_{ti} \quad l_{ti} \quad k_{ti} l_{ti} \quad k_{ti}^2 \quad l_{ti}^2)' , \\ \beta_t = (\beta_{t0} \dots \beta_{t5})' ,$$

and lower case letters (y,l,k) indicate natural logs of upper case letters (Y,L,K). Note that the production frontier changes over time (i.e. β has a time subscript). We impose regularity restrictions to ensure that capital and labor elasticities are nonnegative at all observed input levels. That is:

$$EK_{ti} \equiv \frac{\partial y_{ti}}{\partial k_{ti}} = \beta_{t1} + \beta_{t3} l_{ti} + 2\beta_{t4} k_{ti} \geq 0, \\ EL_{ti} \equiv \frac{\partial y_{ti}}{\partial l_{ti}} = \beta_{t2} + \beta_{t3} k_{ti} + 2\beta_{t5} l_{ti} \geq 0, \quad (3)$$

for all i and t . The elasticity of scale is a reasonable measure of local returns to scale (see Varian (1992), p. 16). For the translog model this takes the form:

$$ERTS_{ti} = EK_{ti} + EL_{ti} = \beta_{t1} + \beta_{t2} + (\beta_{t3} + 2\beta_{t4}) k_{ti} + (\beta_{t3} + 2\beta_{t5}) l_{ti}.$$

In this framework, constant returns to scale correspond to imposing the three restrictions:

$$\beta_{t1} + \beta_{t2} = 1, \quad \beta_{t4} = \beta_{t5}, \quad \beta_{t3} = -2\beta_{t4}.$$

Finally, the frontier will reduce to a Cobb-Douglas specification if we restrict β_{t3} , β_{t4} and β_{t5} to zero. Our specification for the frontier parameters (described in Section 3) allows them to evolve over time in a linear way. This is more general than most specifications in the literature since it allows for technical change to be non-neutral. In preliminary data analysis,

more flexible assumptions (e.g. quadratic) did not seem warranted.

Given the world frontiers in periods t and $t+1$, and the inputs and inefficiencies of country i in both periods, the expected increase in the log of country i 's GDP is:

$$\frac{1}{2} (\mathbf{x}_{t+1,i} - \mathbf{x}_{ti})' (\boldsymbol{\beta}_{t+1} + \boldsymbol{\beta}_t) + \frac{1}{2} (\boldsymbol{\beta}_{t+1} - \boldsymbol{\beta}_t)' (\mathbf{x}_{t+1,i} + \mathbf{x}_{ti}) + (u_{ti} - u_{t+1,i}). \quad (4)$$

where the first term is due to changes in the input use in country i (i.e. changes in allocation and scale), the second term captures the effect of the shift in the frontier (i.e. world technical progress) on the quantity of maximum attainable output for country i , and the third component reflects changes in efficiency of country i . Thus, we define the following theoretically expected annual change in GDP of country i :

$$GC_{t+1,i} = IC_{t+1,i} \times TC_{t+1,i} \times EC_{t+1,i}, \quad (5)$$

which is the product of the annual input change

$$IC_{t+1,i} = \exp\left[\frac{1}{2}(\boldsymbol{\beta}_{t+1} + \boldsymbol{\beta}_t)'(\mathbf{x}_{t+1,i} - \mathbf{x}_{ti})\right], \quad (6)$$

and the annual productivity change

$$PC_{t+1,i} = TC_{t+1,i} \times EC_{t+1,i}, \quad (7)$$

where $EC_{t+1,i} = \exp(u_{ti} - u_{t+1,i})$ is the annual efficiency change (i.e. $\tau_{t+1,i}/\tau_{ti}$) and

$$TC_{t+1,i} = \exp\left[\frac{1}{2}(\mathbf{x}_{t+1,i} + \mathbf{x}_{ti})'(\boldsymbol{\beta}_{t+1} - \boldsymbol{\beta}_t)\right] \quad (8)$$

measures the annual technical change (see KOS). Note that $PC_{t+1,i}$ is the output-based Malmquist productivity change index used in Färe et al. (1994).

Average changes: AGC_i , AIC_i , APC_i , ATC_i , AEC_i are defined as geometric averages of annual changes defined above. To facilitate interpretation, we use average percentage growth rates in our empirical section: $AGG_i = 100 \times (AGC_i - 1)$, $AIG_i = 100 \times (AIC_i - 1)$, $APG_i = 100 \times (APC_i - 1)$, $ATG_i = 100 \times (ATC_i - 1)$, and $AEG_i = 100 \times (AEC_i - 1)$.

3. Bayesian Inference

Following our previous work (see KOS), we assume that the v_{it} 's in (2) are independent Normal random variables with mean 0 and variance σ^2 (unknown) and the u_{it} 's are independent of each other and of the v_{it} 's. The efficiency distribution of $u_{it} = -\ln(\tau_{it})$ must be one-sided to ensure that τ_{it} lies between zero and one, and u_{it} here is taken to be Exponential with mean λ . In order to model the shifts of the frontier in a parsimonious way, we use the linear trend specification for the $J=6$ elements of β_t :

$$\beta_t = \beta^* + t\beta^{**},$$

Thus model (2) can be written as:

$$y = X^* \beta - u + v, \quad (9)$$

where $y = (y_1' \dots y_T')'$, $y_t = (y_{t1} \dots y_{tN})'$; $u = (u_1' \dots u_T')'$, $u_t = (u_{t1} \dots u_{tN})'$; $v = (v_1' \dots v_T')'$, $v_t = (v_{t1} \dots v_{tN})'$; $\beta = (\beta^*, \beta^{**})'$;

$$X^* = \begin{bmatrix} X_1 & X_1 \\ \cdot & \cdot \\ X_t & tX_t \\ \cdot & \cdot \\ X_T & TX_T \end{bmatrix}$$

and $X_t = (x_{t1} \dots x_{tN})'$. Note that β is a $2J \times 1$ vector (where $J=6$).

These assumptions suffice to specify the likelihood function which, when combined with a prior distribution, yields our Bayesian model. Note that we always impose the regularity conditions given in (3) through the prior. Throughout, we use a Uniform prior for β , truncated to ensure that these economic regularity conditions hold at all points in the sample. In order to obtain a well-defined posterior, informative priors must be placed on σ and λ . The use of the traditional flat prior for $\ln(\sigma^2)$ or $\ln(\lambda)$ precludes the existence of the posterior distribution as the marginal data density is then not σ -finite (see Fernández, Osiewalski and Steel (1997)). We elicit the informative prior in such a fashion so as to allow it to be dominated by the sample.

Our Bayesian model is:

$$f_N^{TN}(y | X^* \beta - u, \sigma^2 I_{TN}) p(\beta | X^*) p(\sigma^{-2}) p(\lambda^{-1}) \prod_{t=1}^T \prod_{i=1}^N f_G(u_{ti} | 1, \lambda^{-1}), \quad (10)$$

where

$$p(\lambda^{-1}) = f_G(\lambda^{-1} | 1, -\ln(\tau^*)),$$

$$p(\sigma^{-2}) = \sigma^2 \exp\left(-\frac{s_0}{2\sigma^2}\right),$$

and $p(\beta | X^*) = 1$ if the regularity conditions are satisfied and zero otherwise. In (10), $f_N^M(\cdot | a, B)$ denotes the density function of the M -variate Normal distribution with mean a and covariance matrix B , and $f_G(\cdot | a, b)$ denotes the Gamma density with shape parameter a and scale parameter b , the mean being a/b . We choose $s_0 = 10^{-6}$, which makes the prior density of the symmetric error precision close to the "usual" flat prior on $\ln(\sigma^{-2})$ for small to moderately large values of σ^{-2} : its main effect is to downweigh excessively large values of the precision. Although the prior adopted here is improper, it leads to a proper posterior (see Proposition 1 of Fernández, Osiewalski and Steel (1997)). A detailed justification of, and suggestions for, prior elicitation for λ are given in van den Broeck, Koop, Osiewalski and Steel (1994). It is sufficient to note here that we choose an Exponential prior, and that τ^* is the prior median efficiency, which is a natural quantity to elicit in practice. We typically choose $\tau^* = .75$ (which indicates, *a priori*, that we expect the median of the efficiency distribution to be .75) but we also considered other values for our sensitivity analysis. Unless otherwise specified, $\tau^* = .75$ throughout the paper.

In order to evaluate posterior properties of the models, we use Gibbs sampling methods. (See Gelfand and Smith (1990) and Casella and George (1992) for an introduction). Essentially, Gibbs sampling involves taking sequential random draws from the full conditional posterior distributions. Under very mild assumptions (see e.g. Tierney (1994)), these draws then converge to draws from the joint posterior. Once draws from the joint distribution have been obtained, any posterior feature of interest can be calculated.

Note that the joint posterior density of the parameters and inefficiency terms as well as all conditional posterior densities are proportional to (10). The Gibbs sampler we use for marginal posterior inference draws from analytically tractable conditional posterior

distributions. Details can be found in KOS. The empirical results are based on a sequential Gibbs sampler with 50,000 included and 2,000 burn-in passes. That is, for various starting values, we generated 52,000 passes and discarded the first 2,000 to eliminate possible start-up effects. The reader is referred to Koop, Steel and Osiewalski (1995) for a discussion of various implementations of the Gibbs sampler and techniques for assessing convergence in the context of stochastic frontier models.

4. Empirical Results

We apply our methods to a sample of 22 countries over the period 1980-1990. That is, we include all the countries which are currently (1997) within the European Union, five other Western economies (the U.S., Canada, Australia, Switzerland and Norway), and the two East European countries for which comparable capital stock data were available (Poland and Yugoslavia). Aggregate output (Y) is measured by real GDP; labor (L), by total employment; and capital stock (K) is calculated from capital stock per worker.²

The focus of this paper is on the decomposition of the observed output levels into the frontier and inefficiency terms and on the components of output and productivity growth.

4.1. Model fit, simplifications and robustness

Before going to the economic interpretation and implications of our results, let us discuss the fit of our model and the plausibility of certain simplifications of the translog specification.

In terms of GDP growth rates, the fit is quite good in that observed and expected (AGG) average GDP growth are close for most countries (see Table 5); the difference is usually less than one posterior standard deviation, with the exception of The Netherlands, Portugal and Yugoslavia. Note that Portugal and Yugoslavia represent two extreme growth patterns in the sample (the highest GDP growth and the largest GDP drop, respectively). Moreover, the fit is now not as good as it was in KOS where we used an earlier version of

²This capital stock measure includes gross investment in producer durables and nonresidential construction but excludes residential construction.

the Penn World Tables, a slightly different time period (1979-88) and a smaller group of countries. With the revised data set the results change a lot. This illustrates the fragility of inferences based on highly aggregated international data which are subject to comparability problems and other imperfections.³ However, we shall just use the data that seem the best available and proceed conditionally on them.

In view of our modeling experience from KOS it seems clear that a more general model than our translog specification with a linear trend in its parameters would be overparameterized as we have just 22 countries observed over 11 years. However, we could consider simplified versions of our basic model. If the marginal posterior of β would be Normal, we could easily construct a Highest Posterior Density test for the more restricted versions of our model, by using the fact that the standardized inner product should have a χ^2 distribution. Of course, this Normality does not really hold, but we shall base an approximate χ^2 test on this idea. That should give us at least a rough idea of the appropriateness of certain simplifications. If we then test the restriction of constant returns to scale, we obtain the value 118 for this inner product, which should have an approximate χ^2_6 distribution under the null hypothesis of constant returns to scale, thus strongly corroborating that the simplifying hypothesis of constant returns to scale is not supported by the data. For the hypothesis that the linear trend only affects the constant term β_{10} , we have to compare the value 43.7 with a χ^2_5 distribution, which again leads to very strong rejection of the null, and for the even stronger hypothesis that no trend at all should be present in the LT model, we obtain 56.5 to test for six restrictions. Also, when we test the restrictions leading to the Cobb-Douglas form of the frontier, we have to compare the value 264 with a χ^2_6 posterior distribution. Thus, none of these extra restrictions seem to have any data credibility, and our preferred model will clearly be the full translog model with a linear trend in its parameters.

As discussed earlier, the priors are all quite flat. The key prior hyperparameter is the prior median efficiency, τ^* . We select $\tau^*=0.75$, which implies that the median of the (relatively noninformative) prior efficiency distribution is 0.75. Since this is an important dimension in which to investigate prior sensitivity, we also considered the very different values $\tau^*=0.5$ and $\tau^*=0.9$. The inference on quantities of interest is completely insensitive to

³Note that the Penn World Tables are considered among the best data sets. Yet, comparison of numbers in Version 5.6 and its predecessor reveals that serious changes and corrections have been made.

this prior input.

4.2. Properties of the frontier

The world production frontier shows significant shifts over the relatively short time period under consideration (1980-90), as is evidenced by the strong rejection of the constancy of β_t . This implies both world technical change, which will be discussed later, and changing patterns of factor elasticities and returns to scale calculated for different countries on the basis of this moving frontier.

Table 1 contains the averages over all the periods in the sample, for each country, of the capital and labor elasticities, denoted by EK_{it} and EL_{it} respectively in (3), as well as the returns to scale $ERTS_{it}$ (i.e., the sum of the elasticities), for the different countries and years. It turns out that there is some difference in returns to scale, but most countries indicate increasing returns, with very small standard errors. The exceptions are: Luxembourg, showing decreasing returns to scale, and Switzerland and Norway, both with constant returns. Note that they are all small (in terms of population) and very rich countries. The smallest values of increasing returns to scale are found for Finland, Ireland and Denmark, and then for Belgium, Austria and Sweden. The highest increasing returns to scale are obtained for the two East European economies (i.e., Yugoslavia and Poland) as well as for some large Western countries (the U.S. and the U.K.) and Portugal (which is much smaller, but relatively quite poor). The decomposition over the factors shows much more variability. Capital elasticity ranges from a lowest posterior mean of 0.139 for Switzerland (and 0.155 for Germany) to a high of 0.878 for Yugoslavia (and 0.827 for Portugal). Labor elasticity ranges from 0.241 for Yugoslavia and 0.262 for Portugal to 0.861 for the U.S. and 0.909 for Germany.

For Poland, the average posterior means of both returns to scale (1.115) and capital elasticity (0.702) are the third highest in the sample, and the average posterior mean of labor elasticity is the third lowest (0.413) and nearly the same as for Ireland (0.420).

The countries with the highest capital-labor ratios (Switzerland, Germany and Norway) are exactly those with the lowest capital elasticities. Conversely, the highest values for EK_t are found for Yugoslavia, Portugal and Poland, where the capital-labor ratio is lowest. However, for other (not that extreme) countries this relationship does not hold (e.g., Luxembourg, with the fourth highest K/L, has an average capital elasticity). The situation for labor elasticity is even more complicated. While the lowest values are found for Yugoslavia,

Portugal and Poland, the highest are for Germany, U.S., Switzerland, and then France (the U.S. and France have about average K/L).

Table 2 reports the evolution of the country averages of these quantities over time. There is a clear tendency for EL_t to decrease over time, which is partly offset by an increasing capital elasticity, but the resulting returns to scale $ERTS_t$ is decreasing somewhat over time. Note, incidentally, that we face the situation that returns to scale is much easier to determine than its components as the latter have much larger posterior standard deviations than their sum.

Since returns to scale are not very far from unity, it makes sense to graphically portray a slice from the three-dimensional surface that defines the frontier. Figure 1 plots the output-labor ratio (Y/L) against the capital-labor ratio (K/L) using the posterior means of the frontier parameters, for a labor force of 22.5 million. We have also indicated six countries with labor forces around that number: Canada, Poland, Italy, France, the U.K. and Germany (ordered here according to the size of their labor forces). We would expect countries to lie somewhat below the frontier, although relatively large positive values of the symmetric error component v_{ti} in (2) could lead to the opposite situation⁴. In addition, the frontier as drawn is subject to random variation in β_t . Note that all countries increase K/L from 1980 to 1990 (although Poland only marginally), and that Poland is the only country in the graph that suffers a (small) drop in output per worker over this period.

4.3. Efficiency levels

Table 3 presents year averages of efficiency levels for all countries. The Netherlands and Canada appear to be most efficient, followed by Belgium, Australia and Luxembourg. These countries experienced almost no efficiency change over the period 1980-1990 (see Table 5). For Canada, this situation is graphically depicted in Figure 1⁵. The second group of highly efficient economies (with average efficiency about 0.93) consists of the U.S., Italy, Yugoslavia, the U.K. and Sweden. The third group includes Ireland, Switzerland, Portugal,

⁴However, of the expected squared distance from the frontier, only 5.3% is due to the symmetric disturbance whereas the rest originates from inefficiency.

⁵Since Canada has by far the smallest labor force of the countries plotted in the graph and returns to scale are somewhat increasing (see Subsection 4.2), it will appear slightly less efficient than it should be. For the other countries, such scale effects should be negligible.

France, Austria and Norway (average efficiency in the range 0.89-0.91). Spain and Denmark have efficiencies about 0.86-0.87. Finland and Germany seem to be the least efficient of the analyzed rich countries (0.81 on average), while Greece was even more inefficient (about 0.7). Clearly, Poland shows a particularly low efficiency level (0.45) which is much lower than for any other country in the sample.

Although it may be of interest to look at changes in efficiency levels over time in all countries, we focus on the three poorest economies (see Table 4), which also have the lowest capital-labor ratio, namely Poland, Portugal and Yugoslavia. Interestingly enough, their efficiency levels were changing in three distinct ways.

Portugal's efficiency was about average (0.89) in 1980, then dropped to its minimum level (0.82) in 1984, but since 1985 it was monotonically increasing to the highest level in the sample (0.98) in 1990. Yugoslavia shows a different pattern, going from one of the highest in the sample in 1980 to as low as 0.83 in 1990. The drop in efficiency in 1990 was spectacular, with the former Yugoslavia close to its political and economic disintegration.

Poland shows yet another pattern of efficiencies. From Figure 1 we can already immediately conclude that it was very inefficient both in 1980 and in 1990. It started at the level of 0.44 in 1980 and then went down due to the great political unrest and economic chaos in 1981 and the beginning of 1982.⁶ After the imposition of martial law some moderate steps were taken to improve the economic system (so called "price reform" in 1982 together with allowing state-owned enterprises to base their decisions on profit considerations). However, the central control was not replaced by market forces and the result was a "neither plan nor market" system. The so-called "second stage of reform" started in 1986, leading to further liberalization. All those efforts, although far from being successful, resulted in some increase in efficiency from the lowest level (0.38) in 1982 to the highest (0.51) in 1989, the year of the main political breakthrough. The first results of the "shock therapy" in the beginning of 1990 were stagflationary (see, e.g., Coricelli and Rocha (1991)). In particular, there was a huge drop in production (GDP in 1990 was 85% of that in 1989) with about the same capital and labor as in the previous year, which explains a huge decrease of efficiency, comparable to that in Yugoslavia, but starting from a much lower level.

⁶ The origins of the Polish crisis can be associated with heavy borrowing in the 1970s; see, e.g., Kondratowicz and Okólski (1993). The expected modernization of the economy, financed through foreign capital, did not occur.

In order to give some explanation of the very low efficiency levels for Poland we may notice that the average capital-labor ratio was 7588 for Yugoslavia, 9638 for Portugal and 11462 for Poland, but the average output per worker was 11560 in Yugoslavia, 12484 in Portugal and only 8026 in Poland. Thus, with much more capital per worker Poland produced much less output per worker than each of the two other countries.

It seems that our estimates of efficiency are in perfect agreement with historical experience and the data. However, a rather subtle methodological issue arises: do the estimates for Poland reflect low efficiency or do they just indicate that the country used a different technology ? Unfortunately, these hypotheses are not testable as we have only one country operating on a potentially different frontier. Thus, we can only conclude that our inefficiency estimates for Poland may measure the total productivity (i.e. technological and efficiency) gap with respect to the world leaders.

4.4. Growth decomposition

We have decomposed expected GDP growth into its three components: input growth, technical growth and efficiency growth (measured by AIG, ATG and AEG, respectively). Table 5 presents posterior means and standard deviations of these three measures along with expected GDP growth (i.e. AGG), which is approximately equal to the sum of AIG and APG), actual GDP growth, and productivity growth (i.e. APG, which is approximately ATG+AEG) for the 22 countries under consideration. The standard deviations of most of our average growth measures are very substantial, and thus, our conclusions contain a considerable degree of uncertainty. This is not surprising. Indeed, it would be even more surprising to expect our small and noisy data set to answer the complicated questions about growth decomposition that we are posing with any high degree of accuracy. Average input growth (AIG) is the only quantity with small posterior standard deviations.

A general pattern appears to be that input change and, for most countries, technical change provide the major impetus for growth, and that changes in efficiency play a relatively minor role. For almost all countries, there was either no efficiency change or it was somewhat negative. Two countries that suffered severe decreases in efficiency levels are Yugoslavia and Germany, and the two where efficiency had a positive role to play are Portugal (growing fastest) and the U.K. (growth above average). The efficiency loss for Germany and the gain

for the U.K. can also be inferred directly from Figure 1. For other fast growing countries (Luxembourg, Ireland, Finland, Spain, Canada, Australia and the U.S.), efficiency gains did not appear to play any role in economic growth, and most growth seems to be linked to input changes. The case of Canada is graphically illustrated in Figure 1. Portugal, Spain and the U.K. achieved fast GDP growth largely through input growth, while Luxembourg, the U.S., Finland, Canada, Australia and Ireland relied also on technical change to achieve their fast growth (again, see Figure 1 for Canada). Conversely, for those relatively rich European countries that experienced slower than average GDP growth (i.e. Switzerland, Germany, France, Denmark, The Netherlands, Belgium and Italy), slow growth in inputs would appear to be the culprit since technical change was above average. Germany and, to a lesser extent, France, suffered some decline in efficiency which outweighed their very high technical growth (this can also be seen in Figure 1). In terms of productivity growth, Luxembourg was first, followed by Finland, Ireland, Norway and the U.S., while Yugoslavia, Poland, and, to much lesser extent, Portugal experienced constant decrease of productivity, largely due to negative technical change. As these three countries have the lowest capital-labor ratios, it seems that their input mix was just incompatible with the directions of world technical progress. Indeed, Figure 1 shows that countries with K/L smaller than that of the U.K. will suffer technical regress. Portugal was able to compensate this negative technical change by the huge input change and considerable efficiency improvement (both highest in the sample) and reached the fastest growth, clearly underestimated by our model. However, the East European economies did very poorly. In Yugoslavia, the second highest input growth was completely unproductive due to huge negative technical change and a spectacular drop in efficiency. This pattern of highly negative GDP growth is very difficult to explain through our modeling strategy and thus the model underestimates the actual GDP losses. On the contrary, Poland's moderately negative GDP growth is almost perfectly fitted by our model and it is explained by a poor performance in all three categories: the lowest input change, a highly negative effect of world technical progress and no efficiency improvement.

5. Concluding Remarks

The methodology developed in KOS and applied here has enabled us to estimate the

"world production frontier" and, in particular, efficiency levels of the Polish economy in the period 1980-1990. It also accurately modelled GDP growth and yielded its decomposition into input, technical and efficiency changes. It will be of great interest to apply the same methodology to the data for the 1990s. It seems that the very low efficiency at the beginning of Polish reforms, and thus the possibility of increasing output through efficiency change alone, may explain Poland's fast growth which has been observed in recent years.

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Table 1: Year Averages of Factor Elasticities and Returns to Scale

Country	EK_i	EL_i	$ERTS_i$
Australia	0.338 (0.031)	0.707 (0.030)	1.045 (0.007)
Austria	0.416 (0.027)	0.617 (0.025)	1.033 (0.007)
Belgium	0.369 (0.030)	0.661 (0.029)	1.031 (0.006)
Canada	0.301 (0.037)	0.757 (0.034)	1.058 (0.010)
Denmark	0.426 (0.030)	0.601 (0.028)	1.026 (0.007)
Finland	0.334 (0.036)	0.679 (0.036)	1.013 (0.007)
France	0.307 (0.046)	0.771 (0.042)	1.078 (0.012)
Germany	0.155 (0.063)	0.909 (0.053)	1.063 (0.019)
Greece	0.529 (0.023)	0.519 (0.018)	1.047 (0.011)
Ireland	0.606 (0.044)	0.420 (0.030)	1.026 (0.017)
Italy	0.356 (0.040)	0.724 (0.039)	1.081 (0.011)
Luxembourg	0.418 (0.084)	0.523 (0.081)	0.941 (0.017)
The Netherlands	0.396 (0.026)	0.648 (0.025)	1.045 (0.006)
Norway	0.294 (0.042)	0.708 (0.043)	1.002 (0.008)
Poland	0.702 (0.028)	0.413 (0.042)	1.115 (0.022)
Portugal	0.827 (0.042)	0.262 (0.034)	1.088 (0.029)
Spain	0.466 (0.024)	0.613 (0.028)	1.079 (0.010)
Sweden	0.375 (0.028)	0.659 (0.027)	1.034 (0.006)
Switzerland	0.139 (0.052)	0.858 (0.053)	0.997 (0.016)
U.K.	0.512 (0.033)	0.593 (0.041)	1.105 (0.014)
U.S.	0.257 (0.076)	0.861 (0.070)	1.118 (0.020)
Yugoslavia	0.878 (0.043)	0.241 (0.048)	1.120 (0.032)
average	0.427 (0.040)	0.625 (0.039)	1.052 (0.013)

Table 2: Country Averages of Factor Elasticities and Returns to Scale

Year	EK_t	EL_t	$ERTS_t$
1980	0.402 (0.059)	0.660 (0.058)	1.062 (0.018)
1981	0.407 (0.053)	0.651 (0.052)	1.059 (0.016)
1982	0.412 (0.047)	0.643 (0.046)	1.056 (0.014)
1983	0.420 (0.042)	0.635 (0.041)	1.054 (0.012)
1984	0.427 (0.037)	0.625 (0.036)	1.053 (0.011)
1985	0.434 (0.033)	0.617 (0.032)	1.051 (0.010)
1986	0.439 (0.031)	0.611 (0.030)	1.050 (0.010)
1987	0.441 (0.031)	0.607 (0.030)	1.048 (0.011)
1988	0.442 (0.032)	0.605 (0.031)	1.047 (0.013)
1989	0.440 (0.036)	0.606 (0.034)	1.046 (0.014)
1990	0.436 (0.041)	0.610 (0.039)	1.046 (0.017)
Average	0.427 (0.040)	0.625 (0.039)	1.052 (0.013)

Table 3: Year Averages of Efficiency

Country	Average efficiency
Australia	0.955 (0.030)
Austria	0.891 (0.042)
Belgium	0.958 (0.029)
Canada	0.970 (0.024)
Denmark	0.862 (0.043)
Finland	0.814 (0.041)
France	0.897 (0.042)
Germany	0.809 (0.046)
Greece	0.694 (0.036)
Ireland	0.908 (0.041)
Italy	0.934 (0.037)
Luxembourg	0.945 (0.036)
The Netherlands	0.975 (0.021)
Norway	0.891 (0.043)
Poland	0.450 (0.025)
Portugal	0.898 (0.040)
Spain	0.873 (0.043)
Sweden	0.928 (0.038)
Switzerland	0.905 (0.045)
U.K.	0.928 (0.036)
U.S.	0.935 (0.041)
Yugoslavia	0.932 (0.036)
average	0.880 (0.037)

Table 4: Efficiency Levels for Selected Countries

Year	Portugal	Poland	Yugoslavia
1980	0.890 (0.052)	0.443 (0.027)	0.974 (0.023)
1981	0.875 (0.050)	0.403 (0.024)	0.970 (0.025)
1982	0.871 (0.048)	0.378 (0.021)	0.961 (0.030)
1983	0.842 (0.046)	0.403 (0.022)	0.950 (0.034)
1984	0.822 (0.044)	0.429 (0.023)	0.948 (0.034)
1985	0.847 (0.045)	0.458 (0.025)	0.928 (0.039)
1986	0.890 (0.045)	0.481 (0.026)	0.952 (0.033)
1987	0.938 (0.038)	0.493 (0.027)	0.926 (0.041)
1988	0.955 (0.032)	0.513 (0.028)	0.900 (0.045)
1989	0.968 (0.026)	0.512 (0.029)	0.914 (0.045)
1990	0.980 (0.018)	0.434 (0.025)	0.834 (0.049)

Table 5: Growth Rate Components

Country	GDP growth	AGG	AIG	ATG	AEG	APG
Australia	2.96	3.30 (0.51)	2.65 (0.06)	0.97 (0.23)	-0.33 (0.49)	0.63 (0.50)
Austria	2.12	2.32 (0.60)	2.12 (0.08)	0.87 (0.24)	-0.68 (0.61)	0.20 (0.59)
Belgium	1.89	2.05 (0.38)	1.13 (0.04)	0.96 (0.24)	-0.05 (0.33)	0.91 (0.38)
Canada	2.97	3.34 (0.40)	2.40 (0.13)	1.05 (0.25)	-0.12 (0.35)	0.92 (0.40)
Denmark	2.10	2.11 (0.68)	1.28 (0.04)	0.93 (0.24)	-0.11 (0.71)	0.82 (0.67)
Finland	3.06	3.06 (0.70)	1.79 (0.09)	1.05 (0.30)	0.20 (0.73)	1.25 (0.69)

Country	GDP growth	AGG	AIG	ATG	AEG	APG
France	2.22	2.31 (0.62)	1.66 (0.08)	1.07 (0.29)	-0.43 (0.64)	0.63 (0.61)
Germany	2.14	2.15 (0.68)	1.64 (0.10)	1.64 (0.62)	-1.11 (0.86)	0.51 (0.68)
Greece	1.87	1.87 (0.69)	1.43 (0.04)	0.55 (0.26)	-0.10 (0.73)	0.44 (0.68)
Ireland	3.42	3.14 (0.52)	2.01 (0.10)	0.86 (0.47)	0.24 (0.51)	1.11 (0.50)
Italy	2.14	2.29 (0.52)	1.60 (0.07)	0.84 (0.26)	-0.16 (0.51)	0.68 (0.51)
Luxembourg	3.66	3.88 (0.58)	2.14 (0.24)	1.82 (0.67)	-0.12 (0.47)	1.70 (0.62)
The Netherlands	2.01	2.62 (0.33)	1.86 (0.02)	0.84 (0.22)	-0.10 (0.26)	0.74 (0.33)
Norway	2.44	2.45 (0.67)	1.41 (0.06)	1.06 (0.37)	-0.04 (0.73)	1.02 (0.66)
Poland	-0.76	-0.76 (0.67)	0.88 (0.02)	-1.44 (0.55)	-0.19 (0.86)	-1.63 (0.66)
Portugal	4.25	3.25 (0.57)	3.57 (0.14)	-1.29 (0.52)	0.99 (0.63)	-0.31 (0.58)
Spain	3.06	3.07 (0.64)	2.67 (0.06)	0.34 (0.27)	0.04 (0.66)	0.38 (0.63)
Sweden	2.01	2.21 (0.60)	1.88 (0.07)	0.93 (0.24)	-0.60 (0.60)	0.33 (0.59)
Switzerland	2.06	2.14 (0.60)	1.32 (0.11)	0.97 (0.61)	-0.16 (0.71)	0.80 (0.62)
U.K.	2.85	2.54 (0.58)	1.90 (0.06)	-0.15 (0.45)	0.78 (0.65)	0.63 (0.58)
U.S.	2.64	2.91 (0.61)	1.89 (0.15)	1.53 (0.72)	-0.51 (0.73)	1.00 (0.61)
Yugoslavia	-1.36	-0.63 (0.60)	3.61 (0.13)	-2.57 (0.52)	-1.56 (0.64)	-4.09 (0.57)
average	2.26	2.35 (0.58)	1.95 (0.09)	0.58 (0.39)	-0.19 (0.61)	0.39 (0.57)